

Nucleon Compton scattering in the Dyson-Schwinger approach

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QCD-TNT-III: From quarks and gluons to hadronic matter: A bridge too far?

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Introduction



Goal: compute nucleon's Compton scattering amplitude (and other things) from quark-gluon substructure in QCD.

- Handbag vs. nucleon (s- and u-channel) and meson (t-channel) resonances?
- Quark core vs. pion cloud?
- Electromagnetic gauge invariance at the guark-gluon level?
- Tensor decomposition for (on- and offshell) fermion two-photon vertex?

QCD's Green functions \leftrightarrow "Dyson-Schwinger approach":

Nonperturbative, covariant, low and high energies, light and heavy guarks. But: truncations!

- Baryon spectroscopy from three-body Faddeev equation GE, Alkofer, Krassnigg, Nicmorus, PRL 104 (2010)
- Elastic & transition form factors for N and A GE, PRD 84 (2011); GE, Fischer, EPJ A48 (2012); GE, Nicmorus, PRD 85 (2012); Sanchis-Alepuz et al., PRD 87 (2013), ...
- Tetraguark interpretation for σ meson Heupel, GE, Fischer, PLB 718 (2012)
- Compton scattering GE, Fischer, PRD 85 (2012) & PRD 87 (2013)

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Hadrons: poles in Green functions



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Hadrons: poles in Green functions



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Bethe-Salpeter equations

• Inhomogeneous BSE for quark four-point function:



• Homogeneous BSE for **bound-state wave function**:



 Inhomogeneous BSE for quark-antiquark vertices:



Analogy: geometric series

$$\begin{split} f(x) &= 1 + x f(x) \quad \Rightarrow \quad f(x) = \frac{1}{1-x} \\ |x| &< 1 \quad \Rightarrow \quad f(x) = 1 + x + x^2 + \dots \end{split}$$

What's the kernel K?

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Related to Green functions via **symmetries:** CVC, PCAC \Rightarrow vector, axialvector WTIs

Relate ${\bf K}$ with quark propagator and quark-gluon vertex

Structure of the kernel

Rainbow-ladder: tree-level vertex + effective coupling





√ DCSB, CVC, PCAC

- ⇒ mass generation
- ⇒ Goldstone theorem, massless pion in χ L
- ⇒ em. current conservation
- ⇒ Goldberger-Treiman



Ansatz for effective coupling: Maris, Roberts, Tandy, PRC 56 (1997), PRC 60 (1999)

$$\alpha(k^2) = \alpha_{\rm IR}\left(\frac{k^2}{\Lambda^2}, \eta\right) + \alpha_{\rm UV}(k^2)$$

Adjust infrared scale Λ to physical observable, keep width η as parameter

No pion cloud, no flavor dependence,

no $U_A(1)$ anomaly, no dynamical decay widths



Pion cloud: need infinite summation of t-channel gluons

Mesons

 Pseudoscalar & vector mesons: rainbow-ladder is good. Masses, form factors, decays, ππ scattering lengths, PDFs

Maris, Roberts, Tandy, PRC 56 (1997), PRC 60 (1999); Bashir et al., Commun. Theor. Phys. 58 (2012)

- Need to go beyond rainbow-ladder for excited, scalar, axialvector mesons, η-η', etc.
 Fischer, Williams & Chang, Roberts, PRL 103 (2009) Alkofer et al., EPJ A38 (2008), Bhagwat et al., PRC 76 (2007)
- Heavy mesons Blank, Krassnigg, PRD 84 (2011)



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Baryons

Covariant Faddeev equation: kernel contains 2PI and 3PI parts



Current matrix element: $\langle H|J^{\mu}|H\rangle = \bar{\chi} (G^{-1})^{\mu} \chi$

- Impulse approximation + gauged kernel $\left(G^{-1}\right)^{\mu}=\left(G^{-1}_{0}\right)^{\mu}-K^{\mu}$

'Gauging of equations': Kvinikhidze, Blankleider, PRC 60 (1999)

Oettel, Pichowsky, von Smekal, EPJ A 8 (2000)



Truncation:

- · Quark-quark correlations only (dominant structure in baryons?)
- Rainbow-ladder gluon exchange
- · But full Poincaré-covariant structure of Faddeev amplitude retained
- ightarrow Same input as for mesons, quark from DSE, no additional parameters!

Baryons

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- Impulse approximation + gauged kernel $(G^{-1})^{\mu} = (G_0^{-1})^{\mu} - K^{\mu}$

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Baryon masses

- Good agreement with experiment & lattice. Pion mass is also calculated.
- Same kernel as for mesons, scale set by *f_π*. Full covariant wave functions, no further parameters or approximations.
- Masses not sensitive to effective interaction.
- Diquark clustering in baryons: similar results in quark-diquark approach Oettel, Alkofer, von Smekal, EPJ A8 (200)
 GE, Cloet, Alkofer, Krassnigg, Roberts, PRC 79 (2009)
- Excited baryons (e.g. Roper): also quark-diquark structure?



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Electromagnetic form factors



Nucleon em. FFs vs. momentum transfer GE, PRD 84 (2011)

- Agreement with data at larger *Q*² and lattice at larger quark masses
- Missing pion cloud below 1-2 GeV², in chiral region
- ~ nucleon quark core without pion effects



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Electromagnetic form factors



Nucleon charge radii:

isovector (p-n) Dirac (F1) radius



• Pion-cloud effects missing in chiral region (⇒ divergence!), agreement with lattice at larger quark masses.

Nucleon magnetic moments:

isovector (p-n), isoscalar (p+n)



• But: pion-cloud cancels in $\kappa^s \Leftrightarrow$ quark core Exp: $\kappa^s = -0.12$ Calc: $\kappa^s = -0.12(1)$

Quark-photon vertex

Current matrix element: $\langle H|J^{\mu}|H\rangle =$



Vector WTI $Q^{\mu} \Gamma^{\mu}(k, Q) = S^{-1}(k_{+}) - S^{-1}(k_{-})$ determines vertex up to transverse parts:

 $\Gamma^{\mu}(k,Q) = \Gamma^{\mu}_{\rm BC}(k,Q) + \Gamma^{\mu}_{\rm T}(k,Q)$

 Ball-Chiu vertex, completely specified by dressed fermion propagator: Ball, Chiu, PRD 22 (1980)

 $\Gamma^{\mu}_{\rm BC}(k,Q) = i\gamma^{\mu} \Sigma_A + 2k^{\mu} (i k \Delta_A + \Delta_B)$

$$\begin{split} \Sigma_A &:= \frac{A(k_+^2) + A(k_-^2)}{2}, \\ \Delta_A &:= \frac{A(k_+^2) - A(k_-^2)}{k_+^2 - k_-^2}, \\ \Delta_B &:= \frac{B(k_+^2) - B(k_-^2)}{k_+^2 - k_-^2} \end{split}$$

• Transverse part: free of kinematic singularities, tensor structures $\sim Q, Q^2, Q^3$, contains meson poles Kizilersu, Reenders, Pennington, PRD 92 (1995); GE, Fischer, PRD 87 (2013) $t_{ab}^{\mu\nu} := a \cdot b \, \delta^{\mu\nu} - b^{\mu}a^{\nu}$

Dominant	$\tau^\mu_1 = t^{\mu\nu}_{QQ} \gamma^\nu , \qquad$	$ au_{5}^{\mu} = t_{QQ}^{\mu u} i k^{ u} ,$
	$\tau_2^{\mu} = t_{QQ}^{\mu\nu} k \cdot Q \frac{i}{2} [\gamma^{\nu}, k] ,$	$\tau_6^{\mu} = t_{QQ}^{\mu\nu} k^{\nu} k ,$
Anomalous	$\tau^{\mu}_{3} = \frac{i}{2} \left[\gamma^{\mu}, \mathcal{Q} \right],$	$ au_7^\mu \ = t_{Qk}^{\mu u}k\!\cdot\!Q\gamma^ u, \qquad$ Curtis, Pennington, PRD 42 (1990)
magnetic moment	$\tau_4^{\mu} = \frac{1}{6} \left[\gamma^{\mu}, k, Q \right],$	$\tau_8^{\mu} = t_{Qk}^{\mu\nu} \frac{i}{2} \left[\gamma^{\nu}, \not\!\!\! k \right].$

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⇒ Nonperturbative description of hadron-photon and hadron-meson scattering

Can we extend this to **four-body scattering** processes? GE, Fischer, PRD 85 (2012)



Hadron scattering

Compton scattering, DVCS, 2y physics

 $\bar{p}p \rightarrow \gamma \gamma^*$

annihilation

Meson photo- and electroproduction

Meson production

Nucleon-pion

scattering



Pion Compton scattering

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Nucleon Compton scattering





• RCS, VCS: nucleon polarizabilities



- DVCS: handbag dominance, GPDs
- Forward limit: structure functions in DIS
- Timelike region: pp annhihilation at PANDA
- Spacelike region: two-photon corrections to nucleon form factors, proton radius puzzle?

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Compton scattering





- All direct measurements in kinematic limits (RCS, VCS, forward limit).
- Em. gauge invariance ⇒ Compton amplitude is fully transverse. Analyticity constrains 1PI part in these limits (low-energy theorem).
- Polarizabilities = coefficients of tensor structures that vanish like $\sim Q^{\mu}Q^{\prime\nu}, \ Q^{\mu}Q^{\nu}, \ Q^{\prime\mu}Q^{\prime\nu}, \dots$
- Need tensor basis free of kinematic singularities (18 elements). Complicated...

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Bardeen, Tung, Phys. Rev. 173 (1968)
Perrottet, Lett. Nuovo Cim. 7 (1973)
Tarrach, Nuovo Cim. 28 A (1975)
Drechsel et al., PRC 57 (1998)
L'vov et al., PRC 64 (2001)
Gorchtein, PRC 81 (2010)
Belitsky, Mueller, Ji, 1212.6674 [hep-ph]
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Tensor basis?





Transversality, analyticity and **Bose symmetry** makes the construction extremely difficult...



Tarrach, Nuovo Cim. 28 (1975)

$T_1 = g_{r\mu}$,	$T_{19} = (P_r k_\mu - P_\mu k_{\nu}') \hat{R}$,
$T_{2} = k_{r}k_{\mu}^{'},$	$T_{19} = (P_{\mu}k'_{\mu} + P_{\mu}k_{\theta})\hat{K}$,
$T_z = k_r' k_\mu,$	$T_{\rm so} = \left(P_{\rm s} k_{\rm \mu}^\prime - P_{\rm \mu} k_{\rm s} \right) \hat{K} \; , \label{eq:Tsolution}$
$T_{\mathbf{a}} = k_{\mathbf{r}}k_{\mathbf{s}} + k'_{\mathbf{r}}k'_{\mathbf{\mu}},$	$T_n = P_s \gamma_s + P_s \gamma_s$,
$T_{z} = k_{\rm F}k_{\rm F} - k_{\rm F}^{\prime}k_{\rm F}^{\prime}, \label{eq:Tz}$	$T_{i2} = P_r \gamma_{\mu} - P_{\mu} \gamma_r$,
$T_{\mathbf{e}}=P_{\mathbf{r}}P_{\mathbf{s}},$	$T_{2b}=~k_{\mu}\gamma_{\mu}+k_{\mu}^{'}\gamma_{\pi},$
$T_{\tau} = P_{\tau}k_{s} + P_{\mu}k_{\tau}^{'}, \qquad$	$T_{\rm ss} = -k_r \gamma_\sigma - k'_{\mu} \gamma_{\nu}$,
$T_{s}=P_{r}k_{r}-P_{\mu}k_{r}^{\prime},$	$T_{ii} = k'_r \gamma_{\mu} + k_s \gamma_r$,
$T_{\rm p}=P_{\rm p}k_{\rm p}'+P_{\rm p}k_{\rm r},$	$T_{zs} = k'_r \gamma_\mu - k_s \gamma_r$,
$T_{\rm 10}=P_{\rm F}k_{\rm F}'-P_{\rm F}k_{\rm F},$	$T_{z\tau} = \left(P_{r} \gamma_{\theta} + P_{\mu} \gamma_{r} \right) \hat{K} - \hat{K} (P_{r} \gamma_{\mu} + P_{\mu} \gamma_{r}) ,$
$T_{11}=g_{\rm PP}\hat{I}\!\!\!\!/$,	$T_{20} = \left(P_{\tau} \gamma_{\mu} - P_{\mu} \gamma_{\tau} \right) \hat{R} = \hat{R} \left(P_{\tau} \gamma_{\mu} - P_{\mu} \gamma_{\tau} \right),$
$T_{12}=k_r k_{\mu}' \hat{K}$,	$T_{zz} = \left(k_r\gamma_s + k_{\mu}^{'}\gamma_{\rm e}\right)\hat{K} - \hat{K}\left(k_r\gamma_s + k_{\mu}^{'}\gamma_{\rm e}\right),$
$T_{11} = k_r \dot{k}_\mu \hat{R}$,	$T_{\rm ss} = (k_{\rm r} \; \gamma_{\rm s} - k_{\rm \mu}^{'} \; \gamma_{\rm r}) \hat{K} - \hat{K} (k_{\rm r} \; \gamma_{\rm s} - k_{\rm \mu}^{'} \; \gamma_{\rm r}) , \label{eq:Tss}$
$T_{14} = (k_{\rm F} k_s + k_{\rm F}^{'} k_{\rm F}^{'}) \hat{K}$,	$T_{\rm m} = (k_{\rm r}^{\prime} \; \gamma_{\mu} + k_{\mu} \; \gamma_{\rm r}) \hat{K} - \hat{K} (k_{\rm r}^{\prime} \; \gamma_{\mu} + k_{\mu} \; \gamma_{\rm r}) , \label{eq:Tm}$
$T_{13} = (k_{\rm F} k_{\rm F} - k_{\rm F}^{\prime} k_{\rm F}^{\prime}) \hat{K}$,	$T_{\rm 12} = (k_{\rm r}^{\prime} \gamma_{\rm p} - k_s \gamma_{\rm r}) \hat{K} - \hat{K} (k_{\rm r}^{\prime} \gamma_{\rm p} - k_s \gamma_{\rm r}) , \label{eq:T12}$
$T_{18}=P_{\rm F}P_{\rm S}\hat{R}$,	$T_{\rm m}=~\gamma_{\rm e}\gamma_{\rm e}-\gamma_{\rm e}\gamma_{\rm e},$
$T_{\rm s}, = (P_{\rm r} k_{\rm s} + P_{\mu} k_{\rm r}') \hat{K} \; , \label{eq:Ts}$	$T_{24} = (\gamma_{\tau} \; \gamma_{s} - \gamma_{s} \; \gamma_{t}) \; \vec{K} + \vec{K} (\gamma_{\tau} \; \gamma_{s} - \gamma_{s} \; \gamma_{t}) \; , \label{eq:T24}$

$$\begin{split} r_1 &= h^* K^*_1 - T_1, \\ r_2 &= h^* h^*_1 + h^* K^*_1 - h^*_2 K^*_1 + \frac{h^* - h^*}{2} T_1, \\ r_3 &= h^* h^*_1 K^*_1 + h^* K^*_1 - h^* K^*_1, \\ r_4 &= h^* K (h^* + h^*) T_1 - h^* K T_1, \\ r_5 &= h^* K (h^* + h^*) T_1 - h^* K T_1, \\ r_6 &= h^* K T_1 - h^* K T_1, \\ \frac{h^* - h^*}{4} T_1 + h^* K T_1, \\ \frac{h^* - h^*}{4} T_2 + h^* K T_1, \\ \frac{h^* - h^*}{4} T_1 - h^* K T_1, \\ \frac{h^* - h^*}{4} K T_1 - h^* K T_1, \\ \frac{h^* - h^*}{4} K T_1 - h^* K K T_1. \\ \end{array} \end{split}$$

 $\tau_{ee} = 2P \cdot KT_e - 2Mk \cdot k'T_{ee} + 2MP \cdot KT_{ee} - k \cdot k'T_{ee} + P \cdot KT_{ee}$ $\tau_{11} = -(k^2 - k'^2)T_1 + (k^2 + k'^2)T_1 - 2k \cdot k'T_{11} - 2Mk \cdot k'T_{14} +$ $+ M(k^{2} - k^{\prime 2})T_{22} + M(k^{2} + k^{\prime 2})T_{22} - k \cdot k^{\prime}T_{22} +$ $+ \frac{k^2 + k'^2}{2} T_{11} + \frac{k^2 - k'^2}{2} T_{12},$ $\tau_{is} = -(k^{s} + k'^{s})T_{s} + (k^{s} - k'^{s})T_{s} + 2k \cdot k'T_{s} - 2Mk \cdot k'T_{s} +$ $+ M(k^{i} + k'^{i})T_{ii} + M(k^{i} - k'^{i})T_{ii} - k \cdot k'T_{ii} +$ $+ rac{k^3 - k'^3}{2} T_{31} + rac{k^3 + k'^3}{2} T_{31} ,$ $\tau_{17} = -4P \cdot KT_1 + 2T_1 + 4MT_{11} - 2MT_{15} + T_{22} + k \cdot k'T_{25}$ $\tau_{18} = 4 \bar{T}_{17} - 4 P \cdot K T_{13} + k \cdot k' T_{14}$. $\mathbf{r_{19}} = \frac{1}{\tau_{-12}} \left[2(P \cdot K)^2 \tau_2 + 2k^2 k'^2 \tau_3 - P \cdot K(k^2 + k'^2) \tau_4 - P \cdot K(k^2 - k'^2) \tau_5 \right] =$ $= 2(P \cdot K)^{i} \tilde{T}_{i} + 2k^{i}k'^{i}\tilde{T}_{i} - P \cdot \tilde{K}(k^{i} + k'^{i})\tilde{T}_{i} - P \cdot K(k^{i} - k'^{i})T_{ii},$ $\mathbf{t}_{10} = \frac{1}{(k^2 - k'^2)} [(k^2 - k'^2) \mathbf{t}_{10} - 2(k^2 + k'^2) \mathbf{t}_{14} + 4P \cdot K \mathbf{t}_{13}] =$ $= -2(k^{2}-k^{\prime 2})T_{s}-2P\cdot KT_{1s}+M(k^{2}-k^{\prime 2})T_{ss}+M(k^{2}+k^{\prime 2})T_{ss} -2MP \cdot KT_{24} + \frac{k^2 + k'^2}{2}T_{57} - P \cdot KT_{29} -P \cdot K \frac{k^2 - k'^2}{2} T_{33} + M \frac{k^3 - k'^2}{4} T_{34}$ $\tau_{11} = \frac{1}{(k_1 + k')} [(k^2 + k'^1) \tau_{10} - 2(k^2 - k'^2) \tau_{14} + 4P \cdot K \tau_{24}] =$ $= -2(k^{2} + k'^{2})T_{s} + 2P \cdot KT_{s} + M(k^{2} + k'^{2})T_{s1} + M(k^{3} - k'^{2})T_{s1} -2MP \cdot KT_{10} + \frac{k^2 - k'^2}{2}T_{11} - P \cdot KT_{10} -P \cdot K \frac{k^{3} + k^{'3}}{2} T_{33} + M \frac{k^{3} + k^{'2}}{4} T_{34}$

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Transverse tensor basis for $\Gamma^{\mu\nu}(p,Q,Q')$

- Generalize transverse projectors:
- $t^{\mu\nu}_{\mu} := a \cdot b \,\delta^{\mu\nu} b^{\mu}a^{\nu}$ $\varepsilon_{ab}^{\mu\nu} := \gamma_5 \, \varepsilon^{\mu\nu\alpha\beta} a^{\alpha} b^{\beta}$
- $a, b \in \{p, Q, Q'\}$ (exhausts all possibilities)

Apply Bose-(anti-)symmetric combinations

 $\mathsf{E}^{\mu\alpha,\beta\nu}_{\pm}(a,b) := \frac{1}{2} \left(\varepsilon^{\mu\alpha}_{Q'a'} \, \varepsilon^{\beta\nu}_{bQ} \pm \varepsilon^{\mu\alpha}_{Q'b'} \, \varepsilon^{\beta\nu}_{aQ} \right)$ $\mathsf{F}^{\mu\alpha,\beta\nu}_{\pm}(a,b) := \frac{1}{2} \left(t^{\mu\alpha}_{Q'a'} t^{\beta\nu}_{bQ} \pm t^{\mu\alpha}_{Q'b'} t^{\beta\nu}_{aQ} \right)$ $\mathsf{G}^{\mu\alpha,\beta\nu}_{\pm}(a,b) := \frac{1}{2} \left(\varepsilon^{\mu\alpha}_{O'a'} t^{\beta\nu}_{bO} \pm t^{\mu\alpha}_{O'b'} \varepsilon^{\beta\nu}_{aO} \right)$

to structures independent of Q, Q':

 $\delta^{\alpha\beta}$

 $\delta^{\alpha\beta} \psi$

 $[\gamma^{\alpha}, \gamma$

$$\begin{array}{c|c} & p^{\alpha}\gamma^{\beta} + \gamma^{\alpha}p^{\beta} \\ \hline \delta^{\alpha\beta} & p^{\alpha}\gamma^{\beta} - \gamma^{\alpha}p^{\beta} \\ \hline p^{\alpha}\gamma^{\beta} + \gamma^{\alpha}p^{\beta}, p \\ \hline \left[\gamma^{\alpha},\gamma^{\beta}\right] & \left[p^{\alpha}\gamma^{\beta} - \gamma^{\alpha}p^{\beta}, p\right] \\ \hline \left[\gamma^{\alpha},\gamma^{\beta}, p\right] & p^{\alpha}p^{\beta} \\ \hline p^{\alpha}p^{\beta} p \end{array}$$

- obtain 16 quadratic, 40 cubic 16 quartic terms \Rightarrow 72 in total $\sqrt{}$
- no kinematic singularities √

Transverse onshell basis: GE, Fischer, PRD 87 (2013) & PoS Conf, X (2012)



- Simple
- analytic in all limits
- manifest crossing and charge-conjugation symmetry
- scalar & pion pole only in a few Compton form factors
- Tarrach's basis can be cast in a similar form

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Compton amplitude at quark level

Baryon's **Compton scattering amplitude,** consistent with Faddeev equation: GE, Fischer, PRD 85 (2012)

 $\langle H|J^{\mu}J^{\nu}|H\rangle = \bar{\chi} \left(G^{-1}{}^{\mu}G \, G^{-1}{}^{\nu} + G^{-1}{}^{\nu}G \, G^{-1}{}^{\mu} - (G^{-1})^{\mu\nu} \right) \chi$

In rainbow-ladder (+ crossing & permutation):

 Born (handbag) diagrams: G = 1 + T

G

• all s- and u-channel nucleon resonances:







- crossing symmetry
- √ em. gauge invariance
- ✓ perturbative processes included
- $\sqrt{s, t, u}$ channel poles generated in QCD



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Compton amplitude at quark level



Collect all (nonperturbative!) 'handbag' diagrams, where photon couples to same quark: no nucleon resonances, no cat's ears



- not electromagnetically gauge invariant, but comparable to 1PI, structure part' at nucleon level?
- · reduces to perturbative handbag at large photon momenta
- but also all t-channel poles included!

Represented by full **quark Compton vertex**, including Born terms. Satisfies inhomogeneous BSE:



Solved in rainbow-ladder: 128 tensor structures (72 transverse). Simplifies dramatically by choice of convenient basis!

The 16

t-channel poles



Quark Compton vertex: recovers t-channel poles, e. g. scalar and pion $\sqrt{}$





Quark Compton vertex and **nucleon Compton amplitude:** residues at pion pole recover $\pi\gamma\gamma$ transition form factor $\sqrt{}$



Rainbow-ladder result: Maris & Tandy, PRC 65 (2002)



(extracted from quark Compton vertex)



(extracted from nucleon Compton amplitude)

Here be dragons



General kinematics:

putting quark Compton vertex in nucleon Compton amplitude is not trivial...

- Storage! $\Gamma^{\mu\nu}(p,Q,Q') = \sum_{i=1}^{72} f_i(p^2,Q^2,Q'^2,Q\cdot Q',p\cdot Q,p\cdot Q') \tau_i^{\mu\nu}(p,Q,Q')$
- Angular dependencies ⇒ Chebyshev expansion? Not useful in moving frame Bose & charge-conjugation symmetries ⇒ basis elements have several angular prefactors
- Handbag not gauge-invariant ⇒ incomplete calculation produces singularities in Q², Q^{'2}, Q · Q['], P · Q



Here be dragons



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$\Gamma^{\mu\nu} = \Gamma^{\mu\nu} + \Gamma^{\mu\nu} + \Gamma^{\mu\nu} \cdot 2\text{-pl}$

• Each piece has different transversality properties ⇒ allows to **identify** and remove singularities in nucleon handbag (model ,kinematic rest')

- All these will contribute to Compton form factors
 (⇒ polarizabilities, structure functions, GPDs, etc.). Dominant contributions?
 - ⇒ Born (pure handbag)?
 - \Rightarrow WTI, WTI-T (em. gauge invariance) ?
 - ⇒ Fully transverse part (t-channel poles) ?

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How to defeat dragons

2-photon WTI \Rightarrow general **offshell fermion Compton vertex** can be written as

$\Gamma^{\mu\nu} =$	$\Gamma_{ m B}^{\mu u}$ + Born	- Γ ^{μν} _{BC} WTI	+ $\Gamma_{\rm T}^{\mu\nu}$ WTI-T	 2-photon equivalent of Ball-Chiu vertex, fixed by quark propagator & quark-photon vertex no kinematic singularities but produces singularities in handbag diagrams! 	+	$\Gamma^{\mu u}_{\rm TT}$ Transverse	 not constrained by WTI, calculated from BSE contains t-channel poles no kinematic singularities 72 elements offshell (18 elements onshell) weak angular dependence!
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Polarizabilities: a first look





- α + β: dominated by quark Born terms (pure handbag) (here: 1 / Q·Q' singularity not yet removed)
- β: cancellation between Born and t-channel poles? no singularity in β

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Summary



So far:

- Structure analysis of nucleon Compton amplitude & quark Compton vertex
- Nonperturbative calculation of **handbag part** (quark Compton vertex = Born + t-channel), t-channel pole behavior reproduced.

Next:

- Extract polarizabilities (subtraction needed to restore gauge invariance)
- Two-photon exchange contribution to form factors
- GPDs & nucleon PDFs
- Study offshell effects at nucleon level

Long term:

- Improve truncations (pion cloud, decay channels, quark six-point function)
- Access larger **phase space** (e.g. timelike region in $\,p\bar{p} \to \gamma\gamma$)

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Thanks for your attention.

Cheers to my collaborators:

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